Solutions to exercises

Listed below are the solutions to the exercises.

All solutions are computed using RStudio, though **you should only do the exercises in RStudio if stated in the list of exercises.** This may result in slight differences in numerical answers, which is due to rounding errors.

The solutions may often be computed in different ways and when two solutions are given it does not necessarily mean that more solutions does not exist. However, when two solutions are given we encourage you to think about why these two solutions are equivalent.

```
library(mosaic)
4.3:
a)
a <- 210/885
## [1] 0.2372881
b.i)
b <- 50/210
## [1] 0.2380952
b.ii)
95/675
## [1] 0.1407407
c.i)
50/885
## [1] 0.05649718
c.ii)
## [1] 0.05649718
d)
```

```
yes <- 50/885
no <- 580/885
yes + no
```

[1] 0.7118644

4.5:

a)

The probability distribution is not uniform (all events have the same probability of orcurring). Moreover, the events does not occur with equal probability.

b)

```
0*0.85 + 1*0.13 + 2*0.01 + 3*0.01
```

[1] 0.18

4.11:

Define vector of central probabilities

```
cprob <- c(0.50, 0.90, 0.95, 0.99)
```

Left tail percentiles

```
lprob <- (1 - cprob)/2
lprob</pre>
```

[1] 0.250 0.050 0.025 0.005

Right tail percentiles

```
rprob <- 1 - lprob
rprob</pre>
```

[1] 0.750 0.950 0.975 0.995

z-values for a)-d) in one go without graphics

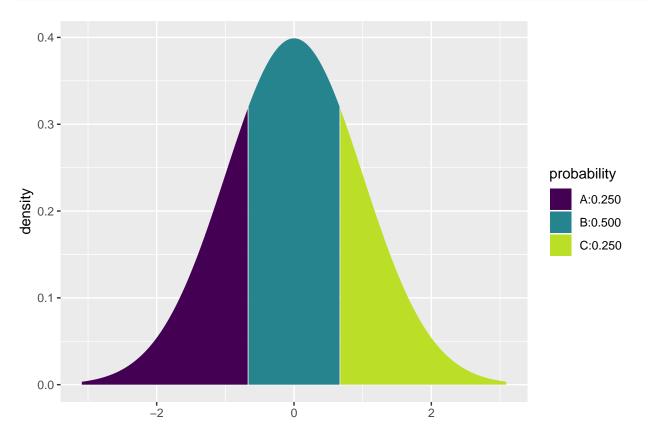
```
qdist("norm", rprob, mean = 0, sd = 1, plot = FALSE)
```

[1] 0.6744898 1.6448536 1.9599640 2.5758293

Graphical solutions:

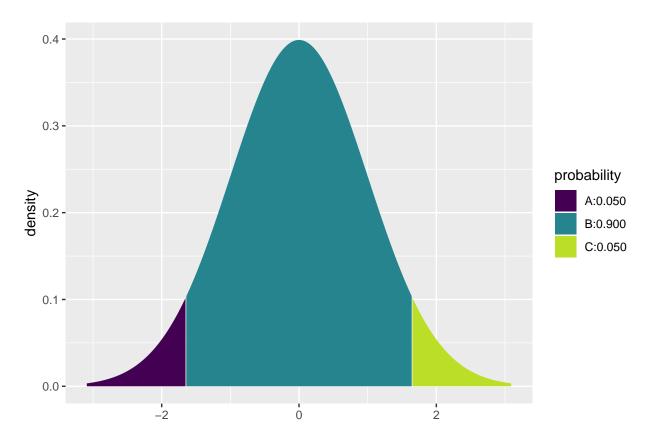
a)

qdist("norm", c(lprob[1], rprob[1]), mean = 0, sd = 1)



[1] -0.6744898 0.6744898

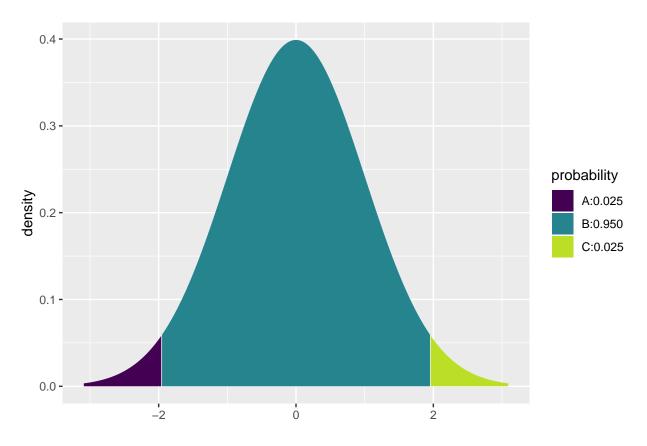
b)



[1] -1.644854 1.644854

 $\mathbf{c})$

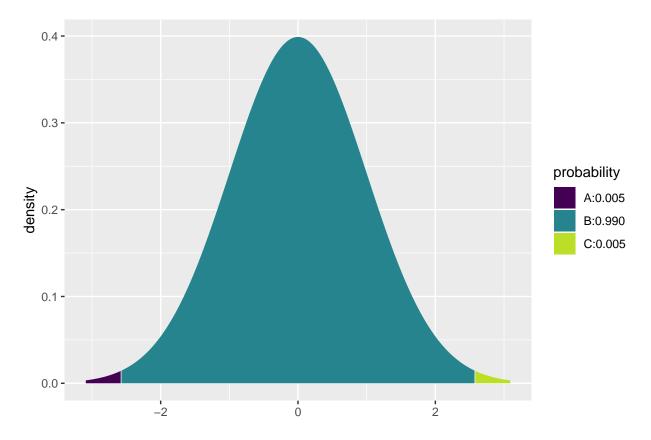
qdist("norm", c(lprob[3], rprob[3]), mean = 0, sd = 1)



[1] -1.959964 1.959964

d)

qdist("norm", c(lprob[4], rprob[4]), mean = 0, sd = 1)



[1] -2.575829 2.575829

4.15:

a)

```
a <- 1 - pdist("norm", 2.1, mean = 0, sd = 1, plot = FALSE)
a
```

[1] 0.01786442

b)

Option 1:

```
b <- a
b
```

[1] 0.01786442

Option 2:

```
b <- pdist("norm", -2.1, mean = 0, sd = 1, plot = FALSE)
b</pre>
```

[1] 0.01786442

```
c)
1 - (a + b)
## [1] 0.9642712
4.33:
a)
Option 1:
pdist("norm", 95, mean = 100, sd = 15, plot = FALSE)
## [1] 0.3694413
Option 2:
pdist("norm", (95 - 100) / 15, mean = 0, sd = 1, plot = FALSE)
## [1] 0.3694413
b)
By CLT, approximately normal with mean 100 and standard deviation 15/sqrt(36) (which is called the
standard error).
se <- 15/sqrt(36)
Option 1:
pdist("norm", 95, mean = 100, sd = se, plot = FALSE)
## [1] 0.02275013
Option 2:
pdist("norm", (95 - 100) / se, mean = 0, sd = 1, plot = FALSE)
## [1] 0.02275013
c)
It is not unusual to see a PDI of 95. This corresponds to a z-score of (95-100)/15 = -0.33, which is not
```

extreme at all.

It is unusual to see a mean PDI of 95 for 36 infants. This corresponds to a z-score of (95-100)/(15/6) = -2. The probability of getting such a low z-score or lower is only 0.0227501.

d) Population distribution (black) and distribution of sample mean (red):

```
se25<-15/sqrt(25)
gf_dist("norm", mean = 100, sd = 15) %>%
gf_dist("norm", mean = 100, sd = se25, color = "red")
```

